

STATISTICAL MECHANICS

- * We know that, thermodynamics is the macroscopic theory of matter \rightarrow concepts are ~~based~~ ^{taken} directly from experiments.
- * Statistical Mechanics \rightarrow Microscopic theory of a system

$$N \rightarrow 10^{23}$$

Hamiltonian $\rightarrow H = \sum_{i=1}^N \frac{\vec{p}_i^2}{2m} + \sum_{\alpha, \beta} V_{\alpha\beta}$ N_0

Hamiltonian $H = \sum_{i=1}^N \frac{\vec{p}_i^2}{2m} + V_0 + \sum_{\alpha, \beta} V_1(\vec{r}_\alpha, \vec{r}_\beta) + \sum_{\alpha, \beta, \gamma} V_2(\vec{r}_\alpha, \vec{r}_\beta, \vec{r}_\gamma) + \dots$

\rightarrow Thermodynamics is described in terms of T, V, N, S, G, \dots

\rightarrow Statistical mechanics description are obtained

starting from microscopic parameters $\{\vec{r}_i, \vec{p}_i\}_{i=1}^N$

Before going into detail of Statistical Mechanics

Course, here I review thermodynamics in short

(1) Thermodynamic system \rightarrow A macroscopic system such as a fluid system,

(ii) state variables / Thermodynamic parameters: —
Pressure, volume, Temperature, entropy, Gibbs free energy, specific heat etc. (of a gas.)


$$P, V, T, S, G, C_p, C_v \text{ ---}$$

(iii) Equation of state: —

A functional relation between thermodynamic parameters —

$$f(T, V, N, P, \dots) = 0$$

For example, Ideal gas case — $PV = RT$

(iv) Extensive quantity → Depend on system size 

(v) Intensive quantity → Independent on system size —
 E, V, N, \dots
 T, P, μ, \dots

vi Laws of thermodynamics: —

- (a) Zeroth law
- (b) First law
- (c) ~~a~~ Second law
- (d) Third law

(a) Zeroth law: — If system A is in equilibrium with system B and C then B is in equilibrium with C

If $T = \text{const.}$ → Thermal equ.

$\mu = \text{const.}$ → Chemical equ.

$P = \text{const.}$ → Mechanical equ.

